

Reg No.: _____

Name: _____

APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

B.Tech S2 (S) / S1 (Challenge Course) Examination December 2025 / January 2026 (2024 Scheme)

Course Code: GAMAT201

Course Name: MATHEMATICS FOR INFORMATION SCIENCE-2

Max. Marks: 60

Duration: 2 hours 30 minutes

PART A

(Answer all questions. Each question carries 3 marks)

- | | | CO | Marks |
|---|---|-----|-------|
| 1 | Find the eigen values of $\begin{bmatrix} 3 & -2 \\ 9 & -6 \end{bmatrix}$ | CO1 | (3) |
| 2 | Find the rank of the matrix $\begin{bmatrix} 3 & 2 & 1 \\ 2 & 1 & 1 \\ 6 & 2 & 4 \end{bmatrix}$ | CO1 | (3) |
| 3 | Determine whether the subset $w = \{(x, x+y, y) : x \text{ and } y \text{ are real numbers}\}$ is a subspace of R^3 . | CO2 | (3) |
| 4 | Show that the set $\{(1,1), (1,-1)\}$ is a basis for R^2 . | CO2 | (3) |
| 5 | Find the unit vector in the direction of $(3,-1,2)$ and verify that the unit vector has length 1. | CO3 | (3) |
| 6 | Find the distance between u and v, if $u = (1,2,0,-3)$ and $v = (3,-2,4,2)$ | CO3 | (3) |
| 7 | Let $T: R^5 \rightarrow R^7$ be a linear transformation. Find the dimension of the kernel of T when the dimension of the range is 2. | CO4 | (3) |
| 8 | Let $T: R^3 \rightarrow R^3$ be a linear transformation such that $T(1,0,0) = (2,-1,4)$, $T(0,1,0) = (1,5,-2)$, $T(0,0,1) = (0,3,1)$ Find $T(2,3,-2)$. | CO4 | (3) |

PART B

(Answer any one full question from each module, each question carries 9 marks)

Module -1

- 9 a) Find the values of α for which the following system is consistent $x+y+z=1$, $x+2y+3z=\alpha$, $x+5y+9z=\alpha^2$ CO1 (5)
- b) Find the eigen vectors of $\begin{bmatrix} 3/2 & 0 \\ 0 & 3 \end{bmatrix}$ CO1 (4)

- 10 a) Solve the system of equations $x+2y+z = 3$, $2x+3y+2z = 5$, $3x-5y+5z = 2$, $3x+9y-z = 4$ using Gauss elimination method. CO1 (5)

- b) Find the matrix of the transformation that diagonalize the matrix $A = \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}$. CO1 (4)

Also write the diagonal matrix.

Module -2

- 11 a) Check whether set of all points on the plane $x+y-2z=0$ is a subspace under standard operation. CO2 (5)

- b) Determine whether the set $\{(0, 0), (1, -1)\}$ is linearly independent or not. CO2 (4)

- 12 a) Given $B = \{(1, 3), (-2, -2)\}$ and $B' = \{(-12, 0), (-4, 4)\}$ are two bases of R^2 , find the transition matrix from B' to B . CO2 (5)

- b) Determine whether the set $S = \{(2, 1), (-1, 2)\}$ spans R^2 . CO2 (4)

Module -3

- 13 a) Find the Least Squares regression line for the data points $(-2,1), (-1,2), (0,1), (1,2), (2,1)$. CO3 (5)

- b) Determine all the vectors v that are orthogonal to u , if $u = (0,5)$. CO3 (4)

- 14 a) Apply Gram-Schmidt orthonormalization process to transform the given bases $B = \{(3,4), (1,0)\}$ into an orthonormal basis. CO3 (5)

- b) Verify the Cauchy-Schwarz inequality for $A = \begin{bmatrix} 1 & -1 \\ 2 & 0 \end{bmatrix}$ $B = \begin{bmatrix} 1 & 1 \\ 0 & 3 \end{bmatrix}$ with inner product $\langle A, B \rangle = a_{11}b_{11} + a_{12}b_{12} + a_{21}b_{21} + a_{22}b_{22}$. CO3 (4)

Module -4

- 15 a) Determine whether the transformation $T: R^2 \rightarrow R^2$ defined by $T(x,y) = (x-y, x+3y)$ is linear. If it is, find the standard matrix of T . CO4 (5)

- b) Find the kernel and range of $T, T: R^2 \rightarrow R^2$ by $T(x) = Ax$ if $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$. CO4 (4)

- 16 a) Find the rank and nullity of $\begin{bmatrix} 1 & 0 & -2 \\ 0 & 1 & -1 \\ 2 & 2 & -6 \end{bmatrix}$. CO4 (5)

- b) Let $T: R^2 \rightarrow R^2$ be a linear transformation defined by $T(x_1, x_2) = (x_1 + x_2, 2x_1 - x_2)$ Find the matrix for T relative to the bases $B = \{(1,2), (-1,1)\}$ and $B' = \{(1,0), (0,1)\}$. CO4 (4)
