Reg No.:

APJ ABDUL KALAM TECHNOLOGICAL UNIVERSIT

B.Tech Degree S4 (R,S) / S2 ((PT) (S, FE) / S4 WP) (R) Examination May

Course Code: MAT206 Course Name: GRAPH THEORY

Max. Marks: 100

9

Duration: 3 Hours

3

PART A Marks (Answer all questions; each question carries 3 marks) 1 Define a regular graph. Draw a regular graph with 4 vertices which is not complete. 3 2 Define an isolated vertex and a pendant vertex with examples. 3 3 3 What is decomposition of a graph? Illustrate with an example. 4 Define a balanced digraph. When will it be regular? 3 What is a relation matrix? Find the relation matrix of the relation "is greater than" 5 3 on the set {2,5,7,9}. 6 Define distance between two vertices in a graph. What is eccentricity of a vertex 3 in a graph? 7 Find the number of pendant vertices in a binary tree with n vertices. 3 8 Define spanning tree of a connected graph. Draw a spanning tree of the following 3 graph.



What is a cut-set of a connected graph G? Define edge connectivity of a graph in 3 terms of its cut-sets.

10 Define a k-chromatic graph. Draw a 2-chromatic graph with 3 vertices.

PART B

(Answer one full question from each module, each question carries 14 marks)

Module -1

11 a) Define isomorphism of two graphs. Check whether the given graphs are 7 isomorphic or not.

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- b) Prove that the maximum number of edges in a simple graph with n vertices is $\frac{n(n-1)}{2}$.
- 12 a) If a graph has exactly two vertices of odd degree, prove that there must be a path 7 joining these two vertices.
 - b) Prove that a simple graph with n vertices and k components can have at most $\frac{(n-k)(n-k+1)}{2}$ edges.

Module -2

13 a) Define Euler graph and Hamiltonian circuit of a graph. Whether the given graph7 has a Hamiltonian circuit? Is the graph Eulerian? Justify your answer.



- b) What is a connected graph? What are the two types of connectedness in digraphs? 7 Give examples.
- 14 a) State and prove a necessary and sufficient condition for a given connected graph 7 to be Eulerian.
 - b) Define simple, symmetric and asymmetric digraphs and give examples for each.

Module -3

- 15 a) Prove that a graph G is a tree if and only if there is one and only one path between7 every pair of vertices in G.
 - b) Find the shortest distance between A and C using Dijkstra's algorithm.



16 a) Prove that every tree has either one or two centers.

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Page 2 of 3

0200MAT206122303

b) Use Prim's algorithm to find the minimal spanning tree of the following graph.

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Module -4

- 17 a) Prove that every circuit has an even number of edges in common with any cut-set. 7
 - b) Prove that the vertex connectivity of any graph G can never exceed the edge connectivity.
- 18 a) Prove that a connected planar graph with n vertices and e edges has e n + 2 8 regions.
 - b) Construct the geometric dual of given graph.



Module -5

19 a) Define incidence matrix of a graph. Write the incidence matrix of following graph.



- b) Prove that if A(G) is the incidence matrix of a connected graph G with n vertices, 7 then the rank of A(G) is n - 1.
- 20 a) Define circuit matrix of a graph. Write the circuit matrix of following graph.



b) Prove that a covering g of a graph is minimal if and only if g contains no paths of 7 length three or more.