

Reg No.: \_\_\_\_\_

Name: \_\_\_\_\_

APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

B.Tech Degree S7 (S, FE) Examination May 2024/ S7 (PT) (S,FE) Examination June 2024 (2015 Scheme)



Course Code: EC401

Course Name: INFORMATION THEORY &amp; CODING

Max. Marks: 100

Duration: 3 Hours

**PART A***Answer any two full questions, each carries 15 marks.*

Marks

- 1 a) Prove that  $H(Y) \geq H(Y/X)$ , where  $H(Y)$  is the marginal entropy and  $H(Y/X)$  is the conditional entropy. (6)
- b) An event has six possible outcomes with the probabilities  $p_1 = 1/2$ ,  $p_2 = 1/4$ ,  $p_3 = 1/8$ ,  $p_4 = 1/16$ ,  $p_5 = 1/32$ ,  $p_6 = 1/32$ . Find the entropy of the system. Also, find the rate of information if there are 16 outcomes per second. (5)
- c) State Shannon's noiseless coding theorem. (4)
- 2 a) Consider a DMS with 7 symbols,  $S_1, S_2, \dots, S_7$  with corresponding probabilities 0.37, 0.33, 0.16, 0.07, 0.04, 0.02 and 0.01. Construct the binary Huffman code and determine the efficiency and redundancy of the code. (8)
- b) State and prove Kraft's inequality for instantaneous code. (7)
- 3 a) A binary channel has the following noise characteristics. (10)
- $$P(Y/X) = \begin{bmatrix} 2/3 & 1/3 \\ 1/3 & 2/3 \end{bmatrix}$$
- Let the input symbols  $x_1$  and  $x_2$  be transmitted with probabilities  $3/4$  and  $1/4$  respectively. Calculate the mutual information, channel capacity, and efficiency of the channel.
- b) Define mutual information and give any three properties of mutual information. (5)

**PART B***Answer any two full questions, each carries 15 marks.*

- 4 a) An analog signal has a bandwidth of 4 kHz. The signal is sampled at 2.5 times the Nyquist rate and each sample quantized into 256 equally likely levels. Assume that successive samples are statistically independent. (10)
- i. Can the output of this source be transmitted without errors over a Gaussian

channel of bandwidth 50 kHz and S/N ratio of 20 dB.

- ii. If the output of this source is to be transmitted without errors over an analog channel of S/N ratio 10dB, compute the bandwidth requirement of the channel.
- b) List any 3 properties of a group. Give 2 examples. (5)
- 5 a) The parity bits of a (8, 4) linear systematic block code are generated by (8)
- $$c_5 = d_1 + d_2 + d_4$$
- $$c_6 = d_1 + d_2 + d_3$$
- $$c_7 = d_1 + d_3 + d_4$$
- $$c_8 = d_2 + d_3 + d_4$$
- (+ sign denotes modulo-2 addition)
- where  $d_1, d_2, d_3$  and  $d_4$  are message bits and  $c_5, c_6, c_7$  and  $c_8$  are parity bits. Find generator matrix  $G$  and parity check matrix  $H$  for this code. Draw the encoder circuit.
- b) Derive the capacity of the Gaussian channel with infinite bandwidth. (7)
- 6 a) The parity check matrix of (7,4) linear block code is given as (10)
- $$H = \begin{bmatrix} 1 & 0 & 0 & 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 1 \end{bmatrix}$$
- i. Find the minimum distance of the code.
- ii. Determine the number of errors this code can detect and correct.
- iii. Suppose that the received codeword,  $r = (1001001)$ . Determine whether the received codeword is in error? If so, obtain the correct codeword.
- b) Derive Shannon's Limit (5)

### PART C

*Answer any two full questions, each carries 20 marks.*

- 7 a) Consider the (7, 4) cyclic code generated by  $g(x) = 1 + x^2 + x^3$ . Draw the systematic cyclic encoder circuit and explain the computation of the code word in systematic form corresponding to the message  $u = 1011$ . (10)
- b) Draw the code tree for a (2, 1, 2) convolutional encoder with the feedback polynomials as  $g^{(1)}(X) = 1 + X + X^2$  and  $g^{(2)}(X) = 1 + X^2$ . (10)
- 8 a) Draw the syndrome computation circuit for a (7, 4) cyclic code with  $g(x) = 1 + x + x^3$ . (5)
- b) Given a (2, 1, 2) convolutional encoder with the feedback polynomials as  $g^{(1)}(X)$  (10)



$=1+X+X^2$  and  $g^{(2)}(X) = 1+X^2$ . Draw a Trellis and find the output sequence for the input sequence [1 0 1 0 1].

- c) Explain the features of BCH codes (5)
- 9 a) Draw a (3,2,1) convolutional encoder with impulse responses given as  $g_1^{(1)} = [1,1]$ ,  $g_1^{(2)} = [0,1]$ ,  $g_1^{(3)} = [1,1]$ ,  $g_2^{(1)} = [0,1]$ ,  $g_2^{(2)} = [1,0]$ ,  $g_2^{(3)} = [1,0]$ . Find the output for input sequence  $u^{(1)} = (101)$  and  $u^{(2)} = (110)$ . (10)
- b) Consider the generator polynomial  $g(X) = 1+ X^3+ X^4+ X^5+ X^6$  of a cyclic code with length 15. Obtain the equivalent generator matrix and parity check matrix of this code. (10)

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