221TCS002122301

Reg No.:\_\_\_\_

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# APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

Name:

First Semester M.Tech Degree Regular and Supplementary Examination December 2023 (2022 Scheme)

# Discipline: COMPUTER SCIENCE AND ENGINEERING

## Course Code & Name: 221TCS002 FOUNDATIONS OF COMPUTER SCIENCE

### Normal Distribution tables are permitted during the examination

Max. Marks: 60

Duration: 2.5 Hours

(5)

(3+4)

Pages: 2

# PART A

# Answer all questions. Each question carries 5 marksMarks1Use mathematical induction to prove that 5 divides n<sup>5</sup>-n whenever n is a non-<br/>negative integer.(5)

2 Is the set of real numbers countable? prove your answer.

3 Solve the recurrence relation  $a_n - 3a_{n-1} = 5.(7^n)$ ,  $n \ge 1$ ,  $a_0 = 2$  (5)

- In a certain factory turning razor blades, there is a small chance of 1/500 for any (5)
  blade to be defective. The blades are in packets of 10. Use Poisson's distribution
  to calculate the approximate number of packets containing
  - (i) No defective blades
  - (ii) One defective blade
  - (iii) Two defective blades respectively in a consignment of 10000 packets.
- 5 In a set of 'm' randomly selected people, what is the probability that at least two (5) people share the same birthday?

#### PART B

#### Answer any 5 questions. Each question carries 7 marks

- 20 students are participating in an after-school program offering classes in Yoga (7)
  Bridge course and Painting. Each student must take at least one of these 3 classes
  but may take 2 or all the 3 classes. Ten students take yoga, 13 students take bridge
  and 9 take Painting. Nine students take at least 2 classes. How many students are
  taking all the 3 courses?
  - (a) Define Pigeon hole principle

7

#### 221TCS002122301

- (b) What is the minimum number of students required in a maths class to be sure that at least 6 will receive the same grade if there are 5 possible grades such as A,B,C,D,E.
- 8 The harmonic numbers  $H_K$ , K = 1,2,3 ... are defined as  $H_K = 1+1/2+1/3+....+1/K$ . Use mathematical induction to show that  $H_{2^N} \ge 1 + N/2$ .
- 9 Determine the number of positive integers 'n' where 1≤ n ≤ 100 and 'n' is not (7) divisible by 2,3, or 5.
- 10 Ram and Sita are planning to apply for a job. The probability that Ram will apply (7) for a job is ¼, Probability that Ram will apply for a job given Sita applies for the job is ½. The probability that Sita applies for a job given that Ram applies is 1/3. Determine the probability that Ram does not apply for the job given that Sita does not apply for the job.
- 11 Prove that the inverse of the product of two elements of a group G is equal to the (7) product of the inverse taken in reverse order.
- 12 Suppose that a person deposits 20000 Rs in a savings account at a bank yielding (7) 11% per year with interest compounded annually. How much will be in the account after 40 years? (Strictly solve the problem using the concept of recurrence relation )

(7)