Reg No.:

Name:

APJ ABDUL KALAM TECHNOLOGICAL UNIVERS

Fifth Semester B.Tech Degree Regular and Supplementary Examination December 2022

Course Code: ECT 307 Course Name: CONTROL SYSTEMS

Max. Marks: 100

Duration: 3 Hours

PART A (Answer all questions; each question carries 3 marks) Marks 1 Compare open loop and closed loop control systems. Give example. (3) 2 Obtain the impulse response of a series RL high pass filter. (3) 3 A unity feedback system has the following forward path transfer function. $G(s) = \frac{180}{s(s+6)}$ and r(t) = 4t. Determine the corresponding static error coefficient (3)and the steady state error. Compare the features of transient and steady state part of a system response. Give an 4 example for a second order control system with natural frequency of 2 rad/s and (3) damping ratio of 0.5. 5 Explain absolute stability and relative stability of control systems. (3) 6 Compare PD, PI and PID controllers. (3)7 Obtain the DC gain of a unity feedback control system whose overall transfer function is given by (3) $T(s) = \frac{10}{(s+3)(s+5)}$ 8 Starting with the principle of argument, state Nyquist stability criterion. . (3) 9 Define state transition matrix. Mention any four properties of it. (3)10 Define the terms state variable and state space. Mention any four distinct advantages (3) of state space representation.

PART B

(Answer one full question from each module, each question carries 14 marks) Module -1

a) Obtain the differential equations governing the mechanical system shown below and (7) draw the *force-current* electrical analogous circuit.

D



b) Find the transfer function of the given system using block diagram reduction method

1



12 a) Obtain the differential equations governing the mechanical system shown below and (7) draw the *force-voltage* electrical analogous circuit



Y

b) Obtain overall transfer function for the given system using Mason's gain formula (7)



Module -2

13 a) A unity feedback system has the following open loop transfer function, where K and T are constants. Determine the factor by which K should be multiplied to reduce the overshoot from 85% to 35%.

$$G(s) = \frac{K}{s(1+sT)}$$

b) Consider a unity feedback control system with the closed loop transfer function given by

 $\frac{C(s)}{R(s)} = \frac{Ks+b}{s^2+as+b}$. Determine the open loop transfer function. Show that the steady (6)

state error in the unit ramp input response is $e_{ss} = \frac{a-k}{b}$

- 14 a) Starting from the generalized transfer function, derive expression for *peak time* of (9) second order under-damped system subjected to unit step function.
 - b) The open loop transfer function of a unity feedback control system is (5)

$$G(s) = \frac{K}{s(s+1)(s+2)}$$

- i) Determine the type and order of the system
- ii) Find the minimum value of K for which the steady state error is less than0.2 for a unit ramp input.

Module -3

15 a) Given the characteristic equation of a system. Using R.H criterion, Find the location of roots in s-plane and hence comment whether the system is fully stable, unstable (5) or conditionally stable.

$$F(s) = s^4 + 2s^3 + 11s^2 + 18s + 18 = 0$$

b) Sketch the root locus for the given open loop transfer function and find the value of (9) K and ω for marginal stability.

$$G(s)H(s) = \frac{K}{s(s+2)(s+3)}$$

a) Given the characteristic equation of a system. Using R.H criterion, Find the range of (6)
K for the system to be stable. Also find the frequency of sustained oscillation at the marginal stability.

$$F(s) = s^4 + 20s^3 + 15s^2 + 2s + K = 0$$

b) Sketch the root locus for the given open loop transfer function and comment on the (8) system stability.

$$G(s)H(s) = \frac{K(s+2)}{s(s+1)(s+4)}$$

Module -4

17 a) Compare lead, lag and lag-lead compensators.

1

b) A unity feedback control system with given G(s), Draw the Bode plot. Find the gain margin and phase margin. Also check for the stability. (Use semi-log sheet) (10)

$$G(s) = \frac{5(1+2s)}{(1+4s)(1+0.25s)}$$

b) Draw the Nyquist plot for the system whose open loop transfer function is

$$G(s)H(s) = \frac{K}{s(s+2)(s+10)}$$

Also comment on closed loop stability.

Module -5

19 a) Obtain the state model for the electrical network shown.



b) Check the controllability and observability of the following system.

$$\dot{X} = \begin{bmatrix} -1 & 0 \\ 0 & -2 \end{bmatrix} X + \begin{bmatrix} 0 \\ 1 \end{bmatrix} U; \quad Y = \begin{bmatrix} 1 & 2 \end{bmatrix} X$$

Page 4 of 5

(4)

(9)

(7)

(7)



20 a) Determine the transfer function of a system represented by

$$\dot{X} = \begin{bmatrix} -2 & -2 \\ 4 & -8 \end{bmatrix} X + \begin{bmatrix} 1 \\ 1 \end{bmatrix} U; \quad Y = \begin{bmatrix} 1 & 0 \end{bmatrix} U$$

b) An LTI system is represented by the state equation $\dot{X} = A X + BU$, where

$$A = \begin{bmatrix} -3 & 0 & 0 \\ 0 & -1 & 1 \\ 0 & 0 & -1 \end{bmatrix} \text{ and } B = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}, \text{ find the state transition matrix } \phi(t).$$