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APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

Sixth Semester B.Tech Degree Regular and Supplementary Examination July 2021



Course Code: EE304

Course Name: ADVANCED CONTROL THEORY

Max. Marks: 100

Duration: 3 Hours

PART A

Answer all questions, each carries 5 marks.

Marks

- 1 Sketch the realisation of a phase lead compensator and derive its transfer function. (5)
- 2 Identify the dominant poles of the unity feedback system with open loop transfer function $G(s) = \frac{168}{(s+2)(s+5)(s+15)}$. (5)
- 3 Compute the solution to the state equation $\dot{x} = \begin{bmatrix} -1 & 0 \\ 0 & -2 \end{bmatrix} x$, $x(0) = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$ (5)
- 4 Sketch the block schematic of a system controlled by a digital controller and list the additional components that appears in a system with digital controller. (5)
- 5 Distinguish between inherent and intentional nonlinearities. Give examples (5)
- 6 Define describing function? What is the assumption that makes the application of describing function analysis? (5)
- 7 List the characteristics that are observed in nonlinear system. (5)
- 8 Identify the equilibrium points for the system $\dot{x}_1 = x_2$, $\dot{x}_2 = -0.5x_2 - \sin(x_1)$. (5)

PART B

Answer any two full questions, each carries 10 marks.

- 9 Design a suitable compensator for the unity feedback system with transfer function $G(s) = \frac{1}{s(s+1)}$ to satisfy the following specifications so that the gain cross over frequency is approximately 1 rad/s. Velocity error constant atleast $10s^{-1}$. Phase margin greater than 40° . (10)
- 10 Design a suitable compensator for the system $G(s) = \frac{3}{s(s+3)}$ to achieve an overshoot less than 20%, settling time less than 1.5s for unit step input. Velocity error constant atleast $5s^{-1}$. (10)

- 11 a) Design a P, PI and PID controller for the system with transfer function (6)
 $G(s) = \frac{20}{s(s+2)(s+10)}$ by applying Zeigler-Nichols tuning method.
- b) Draw the realisation of PID controller and explain its working. (4)

PART C

Answer any two full questions, each carries 10 marks.

- 12 a) Convert the system $\dot{x} = \begin{bmatrix} -1 & 0 \\ 0 & -2 \end{bmatrix} x + \begin{bmatrix} 1 \\ 2 \end{bmatrix} u, y = \begin{bmatrix} 1 & 1 \end{bmatrix} x$ into controllable (5)
 canonical form by applying similarity transformation.
- b) Determine the stability of the system $\dot{x} = \begin{bmatrix} -3 & 7 & 9 \\ 2 & 1 & 3 \\ -4 & -3 & -8 \end{bmatrix} x + \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} u, y = \begin{bmatrix} 1 & 1 & 0 \end{bmatrix} x$. (5)
- 13 a) Design a state feedback controller for the system $\dot{x} = \begin{bmatrix} 1 & 1 \\ 2 & 2 \end{bmatrix} x + \begin{bmatrix} 1 \\ 0 \end{bmatrix} u, y = \begin{bmatrix} 0 & 1 \end{bmatrix} x$ to place the eigen values of the closed loop system matrix at $-2 \pm j2$. (5)
- b) Derive the transfer function of the system $\dot{x} = \begin{bmatrix} -1 & 1 \\ -3 & -2 \end{bmatrix} x + \begin{bmatrix} 1 \\ 0 \end{bmatrix} u, y = \begin{bmatrix} 0 & 1 \end{bmatrix} x$ when the initial state of the system is zero. (5)
- 14 a) Determine the stability of the system with characteristic equation $z^4 + 0.6z^3 + 0.63z^2 - 0.37z + 0.065 = 0$ (6)
- b) Write the structure of state space representation of an n^{th} ordered SISO system (4)
 in digital domain and specify the dimensions of each matrix.

PART D

Answer any two full questions, each carries 10 marks.

- 15 Identify the stability of limit cycle exhibited by the unity feedback system with (10)
 forward transfer function $G(s) = \frac{100}{s(s+2)(s+5)}$ when controlled by an
 amplifier (P-controller) having gain 2 and it saturates when its output reaches
 ± 2 . Also determine the frequency and approximate amplitude of limit cycle.
- 16 Sketch the phase trajectory for the system $\dot{x}_1 = x_2, \dot{x}_2 = u, \text{ where } u = |-x_1|$ (10)
 starting from (0,1).
- 17 Apply lyapunov stability to determine the stability of the autonomous (10)
 system $\dot{x} = \begin{bmatrix} 5 & -12 \\ 7 & -14 \end{bmatrix} x$
