

# APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

08 PALAKKAD CLUSTER

08EE6252C-2-April18

(pages: 3)

Name: \_\_\_\_\_

Reg No: \_\_\_\_\_



SECOND SEMESTER M.TECH. DEGREE EXAMINATION MAY 2018

08EE6252 (C)

DIGITAL CONTROL SYSTEMS

Time: 3 hours

Max. marks: 60

Answer all six questions. Part 'a' of each question is compulsory.

Answer either part 'b' or part 'c' of each question

Q.no.	Module 1	Marks
1.a	Draw the block diagram representation of a digital control system.	3
	<b>Answer b or c</b>	
b	Consider the digital filter designed by	6
	$G(z) = \frac{4(z-1)(z^2+1.2z+1)}{(z+0.1)(z^2-0.3z+0.8)}$ Draw a series and parallel realization diagram.	
c	Obtain the inverse of $X(z) = \frac{z^2+z+2}{(z-1)(z^2-z+1)}$ using partial fraction expansion method.	6

Q.no.	Module 2	Marks
2.a	State and explain Jury's stability criterion.	3
	<b>Answer b or c</b>	
b	Find the range of K for which the system is stable using Jury's stability test	6
	$\frac{K(0.368z + 0.264)}{(z-1)(z-0.368)}$	
c	Obtain the pulse transfer function of the system where G(s) is given by	6

$$G(s) = \frac{1 - e^{-Ts}}{s} \cdot \frac{1}{s(s+1)}$$

**Q.no.** **Module 3** **Marks**

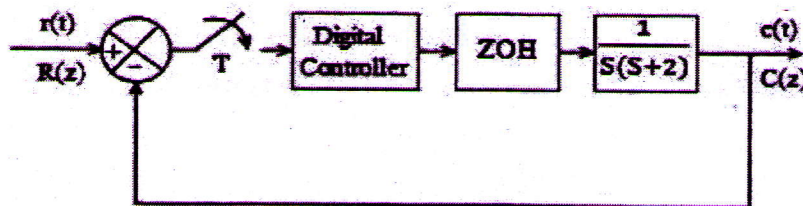
**3.a** Write a short note on the effect of sampling time on the stability of a discrete system. **3**

**Answer b or c**

**b** Explain the design procedure for lead and lag compensators for discrete systems. **6**

**c.** Design a digital controller for the system shown in figure using root locus method to meet the following specifications.

a).  $K_v = 2.5$ , b).  $\zeta = 0.5$ , c)  $T_s \leq 2$  sec.



**6**

**Q.no.** **Module 4** **Marks**

**4.a** What are the Canonical form representations of Discrete Time systems. **3**

**Answer b or c**

**b** Obtain the state variable model for the difference equation  $y(k+3) + 5y(k+2) + 7y(k+1) + 3y(k) = r(k+1) + 2r(k)$  **6**

**c** Obtain the state representation of the following transfer function. **6**

$$\frac{Y(z)}{U(z)} = \frac{5}{(z+2)^2(z+1)}$$

Also obtain the initial values of state variables in terms of  $y(0)$ ,  $y(1)$  and  $y(2)$ . Also draw a block diagram for the same.

**Q.no.** **Module 5** **Marks**

**5.a** What is state transition matrix. Obtain its formulae in z domain. **4**

**Answer b or c**

- b** Obtain the discrete time state and output equation and the pulse transfer function (when the sampling period  $T = 1$ ) of the following **8**

$$G(S) = \frac{Y(S)}{U(S)} = \frac{1}{S(S+2)}$$

- c** Obtain the Controllable Canonical Form (CCF) of the given state space model by using transformation matrix. **8**

$$\begin{bmatrix} x_1(k+1) \\ x_2(k+1) \end{bmatrix} = \begin{bmatrix} 5 & 3 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix} + \begin{bmatrix} 2 \\ 1 \end{bmatrix} u(k)$$

$$y(k) = \begin{bmatrix} 5 & 4 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix}$$

Q.no.	Module 6	Marks
6.a	Define Controllability and Observability for a linear time invariant discrete time control system?	4

**Answer b or c**

- b** Consider the system  $x(k+1) = \begin{bmatrix} 1 & 0 \\ 0 & .5 \end{bmatrix} x(k) + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(k)$ , **8**

$$y(k) = \begin{bmatrix} 1 & 1 \end{bmatrix} x(k)$$

Determine the Observability of the system

- c** Consider the system  $x(k+1) = Gx(k) + Hu(k)$   $y(k) = Cx(k)$  Where **8**

$$G = \begin{bmatrix} 0 & -0.16 \\ 1 & -1 \end{bmatrix} \quad H = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \quad C = \begin{bmatrix} 0 & 1 \end{bmatrix}$$

Design a full order state observer, the desired eigen values of the observer matrix are  $z = 0.5 + j0.5$ ,  $z = 0.5 - j0.5$