B4812



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PART B

Answer any two questions, each carries 15 marks

Determine the exponential Fourier series representation of half wave rectified (10) 4 a) sine wave as shown in the figure below.



- State and prove the Parseval's theorem for continuous time Fourier transforms. b)
- a) Let f(t) be a signal with the spectrum as shown below.



- (i) What is the Nyquist frequency (in Hz) of the signal f(t)?
- the (ii) Suppose signal is sampled by an impulse train $\delta_{Fs}(t) = \sum_{k=-\infty}^{\infty} \delta(t - kT)$ where T is the sampling period and Fs is the sampling frequency. Sketch the spectrum of the sampled signals with (A) Fs = 200 Hz and (B) Fs = 400 Hz. (1)
- (iii)Specify whether the original signal can be recovered from samples in each case (Fs=200 Hz and Fs=400 Hz).
- An LTI system has h(t) such that $\mathcal{L}{h(t)} = H(s) = \frac{1}{s+1}$, $Re{s} > -1$. Determine **b**) (6)the system output y(t) if the input is $x(t) = (e^{-t/2} + 2e^{-t/3}) u(t)$.

6 a) Find the Laplace transform and ROC of the following signals. (9)
(i)
$$e^{-a|z|}, a > 0$$

- (ii) $\sin(\omega_0 t + b)e^{-at}u(t)$ a, b real numbers
- Let $F(\omega) = \mathcal{F}{f(t)}$. Determine the Fourier transform of g(t) = f(at b)in b) (6)terms of $F(\omega)$ where $a \neq 0$, a, b real. Handle the cases for a > 0 and a < 0separately.

PART C

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5

(5)

(2)

(6)

B

9

Answer any two questions, each carries 20 marks

- 7 a) Find the Z transform and ROC of the following signals.
 - (i) $\mathbf{x}[\mathbf{n}] = 2^{n} u[\mathbf{n}]$ (ii) $\delta[\mathbf{n}]$

b) Pole zero plot for Z transform X(z) of a discrete time signal x[n] shown below. (6)



Determine the ROC in each of the following cases.

- (i) x[n] is right sided
- (ii) Fourier transform of x[n] converges

(iii)x[n] is left sided

c) Determine the DTFS coefficients for the discrete time signal $x[n]=cos(\frac{2\pi n}{3})+sin(\frac{2\pi n}{7})$

Also plot the magnitude and phase spectra.

8 a) Consider a LTI system characterised by input output relationship

$$\mathbf{y}[\mathbf{n}] - \frac{1}{4}\mathbf{y}[\mathbf{n} - 1] = \mathbf{x}[n] + \frac{1}{6}\mathbf{x}[n - 1]$$
(2)

- (i) Compute the system function H(z). (2)
 - (ii) Sketch the possible ROCs for H(z).
 - (iii)Compute the impulse response h[n] if it is known that impulse response is (4) left sided.

b) Consider a system with impulse response $h[n] = (0.5)^n u[n]$.

(i) Determine the system function $H(e^{j\omega})$ (4)

(ii) If the input $x[n] = cos(\frac{n\pi}{2})$, determine the output y[n].

a) List any four properties of Z-transform, state and prove the convolution property (10) of Z transforms.

c) A signal
$$x(n)$$
 has DTFT $X(e^{j\omega}) = \frac{1}{1-ae^{-j\omega}} |a| < 1$. Determine the DTFT of
 $x[n+2] e^{j\frac{\pi}{2}n}$. (4)

d) Determine the DTFT of the signal x[n]=u[n]-u[n-N]

(5)

(9)

(8)

(6)