

**SIXTH SEMESTER B.TECH. (ENGINEERING) DEGREE (2014 SCHEME)**  
**EXAMINATION, APRIL 2017**

Electronics and Communication Engineering

EC 14 605—CONTROL SYSTEMS

Time : Three Hours

Maximum : 100 Marks

1. (a) The transfer function of the system is given by :

$$T(s) = \frac{K(s+6)}{s(s+2)(s+5)(s^2+7s+12)}$$

Find (a) Poles ; (b) Zeros ; (c) Pole-zero plot in s-plane.

- (b) Find the closed loop transfer function using Mason's Gain formula for the block diagram in Fig. 1 :

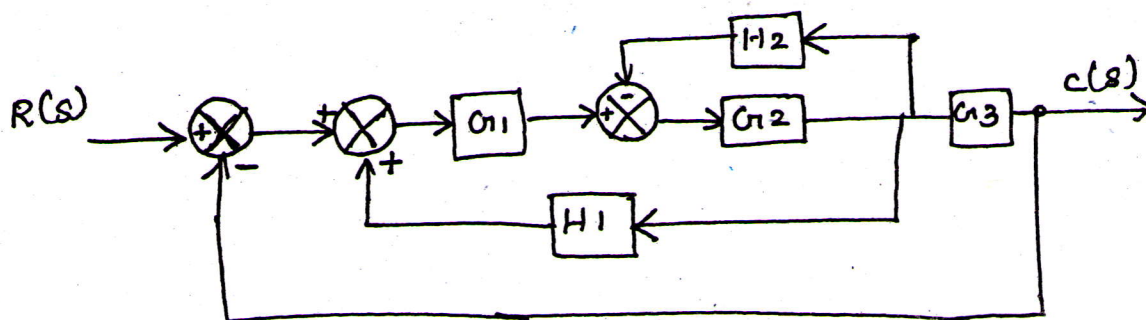


Fig. 1

- (c) Obtain the transfer function of simple RLC series network.

- (d) A second order system is given by :  $\frac{C(s)}{R(s)} = \frac{25}{s^2 + 6s + 25}$ . Find its rise time, peak time, peak overshoot, settling time with respect to unit step input.
- (e) Obtain the step response of the second order system.
- (f) Derive the transfer function of derivative control and explain its effect on the transient response.

Turn over

- (g) Derive the pulse transfer function of open and closed loop data sampled system.
- (h) Analyze the stability of the system using bilinear transformation.
- (i) Derive transfer function from the state model of the system.
- (j) Obtain state transition matrix using Laplace transform for A matrix given below :

$$A = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix}.$$

(8 × 5 = 40 marks)

2. (a) (i) Obtain the transfer function of DC servomotor for speed control.  
 (ii) Compare open loop and closed loop systems.

(10 + 5 = 15 marks)

Or

- (b) (i) Using block diagram reduction technique, find the transfer function from each input to the output for the following system in Fig. 2.

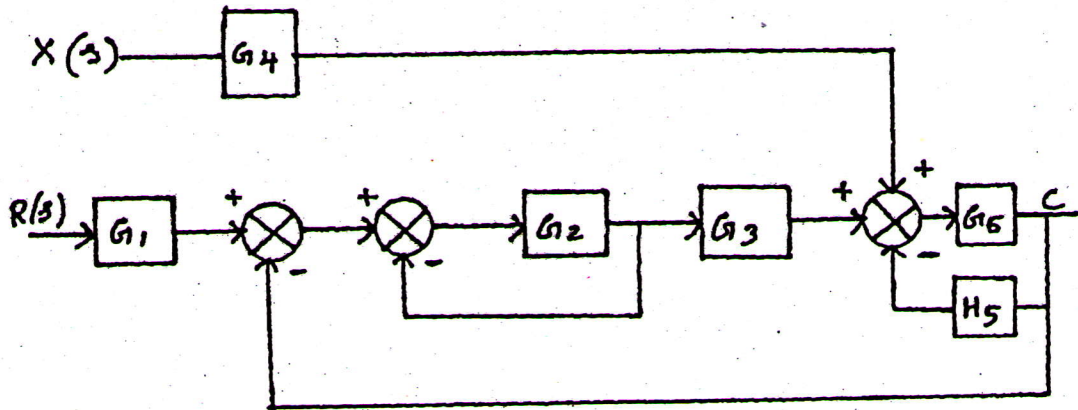


Fig. 2

- (ii) Write the differential equations for the following mechanical system shown in Fig. 3 :

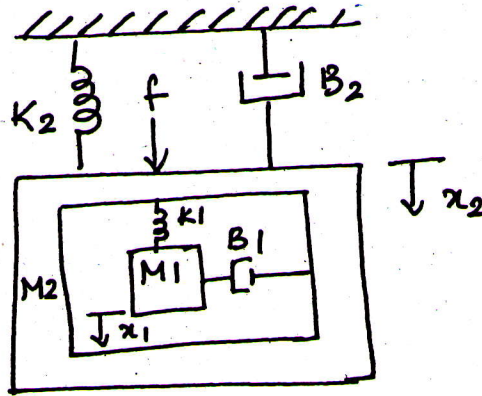


Fig. 3

3. (a) (i) For a closed loop system with  $G(s) = \frac{1}{(s+5)}$  and  $H(s) = 5$ , calculate generalized error coefficients and find the error series.
- (ii) Sketch Bode plot for the following transfer function and determine gain and phase margin :
- $$G(s) = \frac{0.75(1+0.2s)}{s(1+0.5s)(1+0.1s)}$$

(5 + 10 = 15 marks)

Or

- (b) (i) Using Routh Hurwitz criterion, find the stability of  $s^4 + s^3 - 3s^2 + 2 = 0$ .
- (ii) A unity feedback system has an open loop transfer function  $G(s) = \frac{k}{s(s+1)(s+3)}$ . Draw the root locus and determine the value of K.

(5 + 10 = 15 marks)

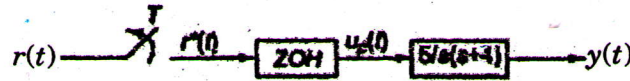
4. (a) Test the stability of the system :

$$F(z) = 2z^4 + 5z^3 + 10z^2 + 2z + 1 \text{ using Jury's criterion and Routh's criterion.}$$

Or

Turn over

- (b) (i) For the system shown below, find the output at the sampling instants  $y(nT)$ . The input is a unit impulse and the sampling period is 0.1 seconds. Also find  $y(nT)$  when  $T \rightarrow \infty$ .



- (ii) Consider a discrete time LTI system described by :

$$y(n) - \frac{3}{4}y(n-1) + \frac{1}{8}y(n-2) = x(n) + \frac{1}{3}x(n-1).$$

Obtain the unit sample response of the system using Z-transform.

5. (a) (i) Explain in detail the state space representation of linear time invariant system with phase variable as forcing function .
- (ii) Obtain the homogeneous solution of the equation  $\dot{x}(t) = Ax(t)$

where  $A = \begin{bmatrix} -9 & 1 \\ -14 & 0 \end{bmatrix}$  and  $x(0) = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$ .

(8 + 7 = 15 marks)

Or

- (b) (i) Diagonalize the following system matrix :

$$A = \begin{bmatrix} 0 & 6 & -5 \\ 1 & 0 & 2 \\ 3 & 2 & 4 \end{bmatrix}.$$

- (ii) What is state transition matrix ? Explain their properties.

(8 + 7 = 15 marks)

[4 × 15 = 60 marks]