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# SIXTH SEMESTER B.TECH. (ENGINEERING) [09 SCHEME **EXAMINATION, APRIL 2016**

AI 09 604 - ADVANCED CONTROL THEORY

**Time : Three Hours** 

## Part A

## Answer all questions.

1. Draw the structure of a full order observer.

2. Distinguish between observable and unobservable systems.

3. List out the properties of a state transition matrix.

4. Write down the transfer function of a PID controller.

5. Define System sensitivity.

## $(5 \times 2 = 10 \text{ marks})$

# Part B

#### Answer any four questions.

- 6. Explain the effects of Pole-Zero cancellation.
- 7. Consider the system :

$$\begin{bmatrix} x_1 (k+1) \\ x_2 (k+1) \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 (k) \\ x_2 (k) \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} (-1)^k$$

$$x_1(0) = 1, x_2(0) = 1 \text{ and } y(k) = x_1(k).$$

Find y(k) for  $k \ge 1$ .

8. Obtain the state model in Jordar canonical form for the transfer function :

$$G(z) = \frac{4z^3 - 12z^2 + 13z - 7}{(z-1)^2 (z-2)}.$$

- 9. Mention the effects of PD control action.
- 10. Determine whether the following quadratic form is negative definite :

$$V(x) = -x_1^2 - 3x_2^2 - 11x_3^2 + 2x_1x_2 - 4x_2x_3 - 2x_1x_3.$$

11. Draw the graphical representation of stable, asymptotically stable and unstable systems in sense of Lyapnov.

 $(4 \times 5 = 20 \text{ marks})$ 

Turn over

# Part C Answer all questions. All questions carry equal marks.

## MODULE I

12. (a) Consider the system :

$$x' = \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \end{bmatrix} u$$
  
and 
$$y = \begin{bmatrix} 2 - 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}.$$

Design a reduced order state observer so that estimation error will decay at least as fast as  $e^{-10t}$ .

- Or
- (b) design a state feedback controller for system  $\vec{x} = \begin{bmatrix} 1 & -1 \\ 1 & -2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 1 \\ 2 \end{bmatrix} u$  to place the poles

#### MODULE II

13. (a) Obtain the transfer function for the following system :

 $\begin{bmatrix} x_1 (k+1) \\ x_2 (k+1) \end{bmatrix} = \begin{bmatrix} 2 & -5 \\ 0.5 & -1 \end{bmatrix} \begin{bmatrix} x_1 (k) \\ x_2 (k) \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u (k) \text{ and } y (k) = 2 x_1 (k).$ 

Or

(b) Consider the characteristic equation  $z^3 + 2.1 z^2 + 1.44 z + 0.32 = 0$ . Determine whether or not any of the roots of the characteristic equation lie outside unit circle centered at origin of z-plane.

#### MODULE III

14. (a) Explain in detail about Ziegler Nichols tuning rules.

Or

(b) Discuss in detail about the effects of composite PID control modes on response of a controlled process.

### MODULE IV

15. (a) Consider the system described by  $x_1^{\bullet} = x_2$  and  $x_2^{\bullet} = x_1 x_2$ . Determine the stability of the system by Lyapunov method.

Or

(b) Explain the design procedure for Robust PID control systems.