

# APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

08 PALAKKAD CLUSTER

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Name:

Reg No:



FIRST SEMESTER M.TECH. DEGREE EXAMINATION DEC 2015

M.Tech- Power Electronics

SYSTEM DYNAMICS

08EE6221

Time:3 hours

Max.marks: 60

Answer all six questions. Part 'a' of each question is compulsory.

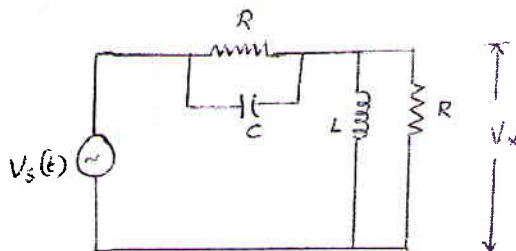
Answer either part 'b' or part 'c' of each question

Q.no.	Module 1	Marks
1.a	Explain the concept of equilibrium points.	3
	<b>Answer b or c</b>	
b	Obtain solution of the state equation	6
	$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$	
	Where u is a unit step function at t=0	
c	Compute state transition matrix and hence the solution of the system where, $Y''' + 6y'' + 11y' + 6y = 6u$	6

Q.no.	Module 2	Marks
2.a	Obtain solution of the state equation for a discrete time system.	3
	<b>Answer b or c</b>	
b	Obtain the state transition matrix of the discrete system	6
	$X(k+1) = \begin{bmatrix} 0 & 1 \\ -10 & -7 \end{bmatrix} X(k)$	
C	Obtain the discrete time state, output equations and pulse T.F of the system	6
	$G(s) = \frac{1}{s(s+2)}$	

Q.no.	Module 3	Marks
3.a	State and prove Lyapunov stability theorem for LTI constant time system	3
<b>Answer b or c</b>		
b	Obtain the Lyapunov function for the state space system $\dot{x} = Ax$ , where	6
$A = \begin{bmatrix} -2 & 1 \\ -5 & 0 \end{bmatrix}$		
c	Using Krasoviski's method, determine the stability of the system $\dot{x}_1 = -x_1 + 2x_2$ and $\dot{x}_2 = -5x_1 - 7x_2$	6

Q.no.	Module 4	Marks
4.a	Derive and explain the condition for Observability.	3
<b>Answer b or c</b>		
b	Test for controllability and observability of a dc motor having transfer function $\frac{10}{s^2(s+1)(s^2+2s+2)}$	6
c	For the circuit given, formulate the state model with the capacitor voltage $v_c$ and inductor current $i_L$ as state variables with source voltage $v_s$ as input and $v_x$ as output. Check controllability condition.	6



Q.no.	Module 5	Marks
5.a	Explain the concept of state feedback controllers .	4
<b>Answer b or c</b>		
b	Design a state feedback controller to yield a percentage overshoot of 20.8 and	8

setting time of 4 seconds for a plant.  $G(s) = \frac{s+4}{(s+1)(s+2)(s+5)}$ .

- c Consider a system described by the transfer function  $\frac{s^2+2s+50}{s(s+4)(s+6)}$  Design 8
- A full order observer for the system with poles  $s=-10,-10,-10$
  - A reduced order observer with poles  $-10$  and  $-10$

Q.no.	<b>Module 6</b>	<b>Marks</b>
6.a	Obtain the optimal state regulator problem.	4

**Answer b or c**

- b A continuous time system is given by  $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 2 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} u$  and  $y=cx$ . Solve 8
- matrix Riccati equation that results in control signal that minimizes the performance index.  $\int_0^5 [y^T(t)y(t) + u^T(t)u(t)]dt$ . Solve for  $C_1=[0 \ 1]$  and  $C_2=[1 \ 0]$  and complete the results.

- c For a second order unity feedback system with open loop transfer function  $G(s)=\frac{10}{s(s+a)}$ , determine 'a' that will minimise the performance measure  $J=\int_0^a [x^T Q x]dt$  8
- when the input is a unit step.