FIFTH SEMESTER B.TECH. (ENGINEERING) (19)

AI 09 502—SIGNALS AND SYSTEM

Time: Three Hours



Answer all questions.

- 1. What is a discrete time signal? Give an example.
- 2. What is sampling?
- 3. Find the Laplace transform of x(t) = u(t).
- 4. Find the initial value $x(0^+)$ for Laplace transform $X(s) = 3/(s^2 + 5s + 1)$.
- 5. What is meant by Region of convergence?

 $(5 \times 2 = 10 \text{ marks})$

num: 70 Marks

Part B

Answer any four questions.

- 6. Check whether the system y(t) = Ax(t) + B is static/dynamic, Linear/non linear and Time variant/invariant.
- 7. Obtain the differential equation of a series RLC circuit having a source of v(t).
- 8. Explain about Hilbert Transform.
- 9. Find the Fourier Transform of $x(t) = e^{-2t} u(t)$.
- 10. Find the inverse z transform of $X(z) = \cos(3z)$.
- 11. Determine the Laplace Transform and ROC for x(t) = tu(t).

 $(4 \times 5 = 20 \text{ marks})$

Part C

- 12. Sketch the following signals:
 - (i) 2u(t+2)-2u(t-3).
- (ii) u(t+4)u(t+4).

(iii) r(-t)u(t+2).

- (iv) r (-0.25t + 1).
- (v) r(t)-r(t-1)-r(t-3)+r(t-4).

Or

- 13. (a) Check whether the following systems are causal or not
 - (i) $y(t) = x^2(t) + x(t-2)$
- (ii) $y(n) = x(n^2)$.
 - (iii) y(n) = 2x(n) + x(n-3).

(4½ marks)

- (b) Find the convolution of x(n) = u(n) 2u(n-3) + u(n-6) and h(n) = u(n+2) u(n-9) (5½ marks)
- 14. (a) Derive the transfer function of a system for distortion less transmission through the LTI system.

(6 marks)

(b) Determine the energy spectral density of a function of width τ and amplitude A. (4 marks)

Or

15. (a) Determine the response of the system characterized by the impulse response $h(n) = (1/2)^n$ u(n) to the input signal $x(n) = 2^n u(n)$.

(6 marks)

(b) Explain about the transmission of a rectangular pulse through an ideal Low pass filter.

(4 marks)

16. (a) Derive the Fourier series for a halfwave rectifier.

(6 marks)

(b) Determine the system function of the LTI system with $x(t) = e^{-3t} u(t)$ and $y(t) = (e^{-t} - e^{-2t}) u(t)$.

(4 marks)

Or

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17. (a) Determine the system function of the LTI system with the following information. The system is rational, causal and has two poles at s=4. If x(t)=1 then y(t)=0. The value of the impulse response at $t=0^+$ is 4.

(4 marks)

(b) Derive the Fourier series of a triangular signal with a period T.

(6 marks)

18. (a) Explain the properties of Z Transform.

(6 marks)

(b) Find the Z transform of $x(n) = (1/2)^n u(n)^* (1/4)^n u(n)$.

(4 marks)

Or

19. (a) A causal system is represented by H $(z) = z + 2/(2z^2 - 3z + 4)$. Find the difference equation and frequency response of the system.

(6 marks)

b) Plot the pole-zero pattern of y(n) = 2y(n-1)0.8y(n-2) + x(n) + 0.8x(n-1). Comment on it's stability.

(4 marks)

 $[4 \times 10 = 40 \text{ marks}]$