

# FOURTH SEMESTER B.TECH. (ENGINEERING) DEGREE APRIL 2013

ME 09 403/PTME 09 402-MECHANICS OF SOLIDS

(2009 Scheme)

[Regular / Improvement / Supplementary]

Time: Three Hours

Maximum: 70 Marks

#### Part A

### Answer all questions.

- 1. Show that the volumetric strain of a body is the algebraic sum of the linear strains in three mutually perpendicular directions.
- 2. Derive an expression for the shear stress produced in a circular shaft subjected to torsion.
- 3. State the assumptions involved in the theory of simple bending.
- 4. Define and explain principal planes and principal stresses.
- 5. Write the assumptions made in Euler's theory of columns. Also mention its limitations.

 $(5 \times 2 = 10 \text{ marks})$ 

#### Part B

## Answer any four questions.

- 1. Define stress, strain and elasticity. Derive a relation between stress and strain of an elastic body.
- 2. Show that the volumetric strain of a body is the algebraic sum of the linear strains in three mutually perpendicular directions.
- 3. Derive an expression for the shear stress produced in a circular shaft which is subjected to torsion. What are the assumptions made in the above derivation?
- 4. The maximum shear stress experienced by a shaft of diameter 70 mm is 70 MPa. Compute shear stress at a point where the radius of 35 mm.
- 5. Explain Maximum principal strain theory, Maximum strain energy theory of failure that governs the design of a stressed system.
- 6. Derive the Eulers formula for a column hinged at both ends.

 $(4 \times 5 = 20 \text{ marks})$ 

#### Part C

1. Three bars made of Copper, Zinc and Aluminum are equal length and have cross-sectional areas of 400, 800 and 1200 mm<sup>2</sup> respectively. They are rigidly connected at their ends. If compound member is subjected to a longitudinal pull of 350 kN, estimate the proportion of load carried by each bar and induced stresses. Take elastic moduli of Copper, Zinc and Aluminum to be 1.2 × 105 N/mm<sup>2</sup> 1.0 × 105 N/mm<sup>2</sup> and 0.89 × 105 N/mm<sup>2</sup> respectively.

- 2. The modulus of rigidity of a material is  $0.8 \times 105 \text{ N/mm}^2$ . When a 6 mm  $\times$  6 mm rod of this material was subjected to an axial pull of 3600 N it was found that the lateral dimension of the rod changed to 5.9991 mm  $\times$  5.9991 mm. Find the Poisson's ratio and the modulus of elasticity.
- 3. A solid circular shaft transmits 75 KW at 200 r.p.m. Calculate the shaft diameter if the twist in the shaft is not exceed 10 in 2 metres length of shaft and the shearing stress is limited to 50 N/mm<sup>2</sup>. Take  $C = 1 \times 10^5 \text{ N/mm}^2$ .

Or

4. Draw shear force bending moment diagrams for the cantilever beam shown in Fig. 1.

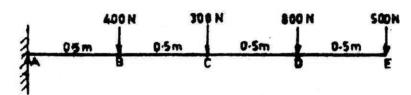


Fig. 1.

5. Two wooden planks 150 mm × 50 mm each are connected to form a T-section of a beam. If the movement of 3.4 kNm is applied around the horizontal neutral axis, inducing tension below the neutral axis, find the stresses at the extreme fibers of the cross-section. Also calculate the total tensile force on the cross-section.

Or

- 6. A steel girder of uniform section, 14 metres long is simply supported at its ends. It carries concentrated loads of 90 kN and 60 kN at two points 3 metres and 24.5 meters from the two ends respectively. Calculate:
  - (a) The deflection of girder at the points under the two loads;
  - (b) The maximum deflection

Take  $E = 200 \text{ GN/m}^2$ .

7. The A rectangular block of material is subjected to a tensile stress of 100 N/mm<sup>2</sup> on a one plane and a tensile stress of 50 N/mm<sup>2</sup> on a plane at right angles, together with shear stresses of 60pa on the same planes.

Find:

- (a) The direction of the principal planes
- (b) The magnitude of the principal stress.
- (c) The magnitude of the greatest shear stress.

Or

8. A column with one end hinged and other end fixed has a length of 5 m. and a hollow circular cross-section of outer diameter 100 mm. and wall thickness 10 mm. If  $E = 1.6 \times 105 \text{ N/mm}^2$ , and crushing strength  $f = 350 \text{ N/mm}^2$ , find the load that the column may carry with a factor of safety of 2.5 according to Euler theory and Rankine-Gordon theory. Take  $\alpha = 1/4500$ .

 $(4 \times 10 = 40 \text{ marks})$