

C 26471

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Name.....

Reg. No.....

COMBINED FIRST AND SECOND SEMESTER B.TECH. (ENGINEERING)  
DEGREE EXAMINATION, APRIL 2012

PTEN/EN 09 102—ENGINEERING MATHEMATICS - II

Time : Three Hours

Maximum : 70 Marks

Part A

Answer all questions.

1. Solve  $(x^2 - ay) dx = (ax - y^2) dy$

2. Find the Laplace transform of

$$f(t) = k, 0 \leq t \leq a$$
$$= -k, a \leq t \leq 2a$$

and  $f(t + 2a) = f(t) \forall t$ .

3. Find grad  $\phi$  if  $\phi = (y^2 - 2xyz^3) \hat{i} + (3 + 2xy - x^2 z^3) \hat{j} + (6z^3 - 3x^2 y z^2) \hat{k}$ .

4. If  $\vec{k} = (x^2 + y^2 + 2xz) \vec{i} + (xz - xy + yz) \vec{j} + (z^2 + x^2) \vec{k}$ , find  $\nabla \cdot \vec{F}$ .

5. Evaluate  $\int_C \phi d\vec{r}$ , where C is the curve  $x = t, y = t^2, z = (1 - t)$  and  $\phi = x^2 y(1 + z)$  from  $t = 0$  to  $t = 1$ .

(5 × 2 = 10 marks)

Part B

Answer any four questions.

6. Solve  $\frac{y}{x} \frac{dy}{dx} + \frac{x^2 + y^2 - 1}{2(x^2 + y^2) + 1} = 0$ .

7. Solve  $L \left\{ \sin h \frac{t}{2} \sin \frac{\sqrt{3}}{2} t \right\}$

Turn over

9. Find the angle between the surfaces  $x^2 - y^2 - z^2 = 11$  and  $xy + yz - zx = 18$  at the point  $(6, 4, 3)$ .
10. Evaluate  $\int_C (x^2 - y^2) dx + 2xy dy$  where  $C$  is the boundary of the rectangle in the  $xy$ -plane bounded by the lines  $x = 0, x = a, y = 0$  and  $y = b$ .
11. Use Gauss divergence theorem for  $\vec{F} = x^2 \vec{i} + y^2 \vec{j} + z^2 \vec{k}$ , where  $S$  is the surface of the cuboid formed by the planes  $x = 0, x = a, y = 0, y = b, z = 0$  and  $z = c$  for evaluating  $\iint_S \vec{F} \cdot d\vec{S}$ .

(4 × 5 = 20 marks)

**Part C***Answer section (a) or section (b) of each question.*

12. (a) Solve  $(D^2 - 4D + 4)y = 8x^2 e^{2x} \sin x$

*Or*

(b) Solve the equation  $(x^2 + 1) \frac{dy}{dx} + 4xy = \frac{1}{x^2 + 1}$  by using method of variation of parameter.

13. (a) Find the Laplace transform of  $\int_0^\infty \left( \frac{\cos at - \cos bt}{t} \right) dt$ .

*Or*

(b) Find the inverse Laplace transform of  $\frac{s^2 + 8s + 16}{(s^2 + 6s + 10)^2}$ .

14. (a) Show that  $\vec{F} = (y^2 - z^2 + 3yz - 2x)\hat{i} + (3xz + 2xy)\hat{j} + (3xy - 2xz + 2z)\hat{k}$  is both solenoidal and irrotational.

Or

- (b) If  $u$  and  $v$  are scalar point functions and  $\vec{F}$  is a vector point function such that  $u\vec{F} = \nabla v$ , prove that  $\vec{F} \cdot \text{curl } \vec{F} = 0$ .

15. (a) If  $S$  is a closed surface enclosing a volume  $V$ , evaluate  $\iint_S \nabla(r^2) \cdot d\vec{S}$

Or

- (b) Use Green's theorem in a plane to find the area of the region in the  $xoy$ -plane bounded by  $y^3 = x^2$  and  $y = x$ .

(4 × 10 = 40 marks)