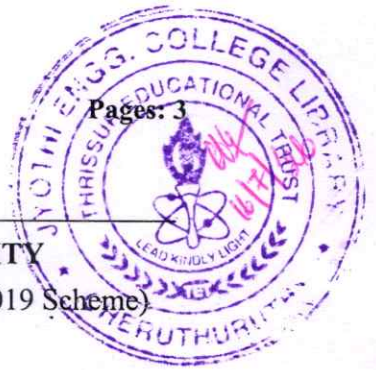




Reg No.: _____

Name: _____

APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

B.Tech Degree S4 (S,FE) (FT/WP/PT) Examinations April/May 2026 (2019 Scheme)

Course Code: ECT204**Course Name: SIGNALS AND SYSTEMS**

Max. Marks: 100

Duration: 3 Hours

PART A*(Answer all questions; each question carries 3 marks)*

Marks

- | | | |
|----|--|---|
| 1 | Determine whether the signal $x(t) = 5e^{-2t}u(t)$ is an energy or power signal. | 3 |
| 2 | Compute the output sequence of an LTI system with impulse response, $h(n)=[3, 2]$ to the input $x(n)=[1, 3, 2, 1]$? | 3 |
| 3 | State the Dirichlet's conditions for the convergence of Fourier series. | 3 |
| 4 | Explain Gibbs phenomenon observed in Fourier series. | 3 |
| 5 | State sampling theorem for low pass signals and mention its significance | 3 |
| 6 | Determine the Nyquist rate for the signal $x(t) = 1 + \cos 2000\pi t + \sin 4000\pi t$ | 3 |
| 7 | Determine the magnitude spectrum $ X(e^{j\omega}) $ of $x[n]=\{1,2,1\}$. | 3 |
| 8 | Write any three properties of DTFS. | 3 |
| 9 | Define the relation between DTFT and Z-transform. | 3 |
| 10 | Find the Z-transform and ROC of $x(n)=a^n u[n]; a < 1$. Does the Fourier transform exist for this signal? | 3 |

PART B*(Answer one full question from each module, each question carries 14 marks)***Module -1**

- 11 a) Consider the continuous-time system described by the differential equation: 8

$$\frac{dy}{dt} + 3y(t) = x(t - 2)$$

- (a) Represent the system using a proper block diagram from the differential equation.
(b) Determine whether the system is linear, time-invariant, and causal. Justify each answer based on the given equation.

- b) Two continuous-time signals are: $x(t) = u(t) - u(t - 2)$ and $y(t) = u(t - 1) - u(t - 3)$. Compute the cross-correlation and sketch it. 6
- 12 a) A continuous-time LTI system has impulse response $h(t) = e^{-2t}u(t)$ and the input signal is $x(t) = u(t) - u(t - 2)$. Determine the output signal and sketch the 8

waveform.

- b) A discrete-time system is described by:

6

$$y[n] = x[n] - x[n-2]$$

(a) Test whether the system is linear, time-invariant, and causal. Provide proper reasoning for each property.

(b) For the input $x[n] = \{1, 2, 3\}$, sketch the shifted version $x[n-2]$ used in the system equation.

Module -2

- 13 a) Find the complex exponential Fourier Series representation of the given signal 7

$$x(t) = \cos 4t + \sin 6t$$

- b) Determine the Laplace transforms of the following sinusoidal function 7

$$x(t) = A \sin \omega t \cdot u(t)$$

- 14 a) Find the Fourier Transform of 8

$$(1) x(t) = t^2 u(t) \cdot u(t-f) \text{ and}$$

$$(2) x(t) = t \exp(-at) u(t); a > 0$$

- b) State and prove multiplication property of Fourier transform 6

Module -3

- 15 a) A continuous-time LTI system is described by the differential equation: 8

$$\frac{d^2 y(t)}{dt^2} + 5 \frac{dy(t)}{dt} + 6y(t) = x(t)$$

(a) Determine the transfer function $H(s)$.

(b) Using pole locations, determine whether the system is BIBO stable and justify.

- b) A continuous-time signal is 6

$$x(t) = \cos(200\pi t) + \cos(600\pi t)$$

(i) Determine the Nyquist sampling interval.

(ii) If the signal is sampled at $F_s = 400 \text{ Hz}$, determine the apparent (aliased) frequencies in the sampled spectrum and comment on aliasing.

- 16 a) Using Laplace transform, obtain response for the LTI system with 8
impulse response $h(t)$ and input $x(t)$ where

$$h(t) = e^{-2t}u(t), \quad x(t) = u(t),$$

- b) Derive Sampling Theorem for low-pass signals.

6

Module -4

- 17 a) State and prove time shifting and convolution property of DTFT.

9

- b) Find the inverse Laplace transform of $X(s) = \frac{-5s-7}{(s+1)(s-1)(s+2)}$ with

5

$$\text{ROC } -1 < \text{Re}(s) < 1$$

- 18 a) Determine the convolution of the signals given below using Fourier Transform.

8

$$x_1(n) = \left(\frac{1}{2}\right)^n u(n); \quad x_2(n) = \left(\frac{1}{3}\right)^n u(n)$$

- b) Determine the DTFT of the following signals, given $x(n)$ has a DTFT $X(e^{j\omega})$. Specify the ROC also.

6

(1). $y[n] = x(2-n)$

(2). $y[n] = Ax(n) \cos \frac{1}{3} \pi n$

Module -5.

- 19 a) The step response of a discrete time LTI system is given by $s[n] = a^n u[n]$;

7

$0 < a < 1$. Find impulse response $h[n]$ of the system using z-transform.

- b) Obtain z-transform of $x(n) = a^n \sin(\omega_0 n) u(n)$.

7

- 20 a) Find inverse z-transform of $X(z)$ using power series expansion technique.

7

$$X(z) = \frac{z}{2z^2 - 3z + 1}; \quad z > 1.$$

- b) A causal system is represented by the following difference equation: $y(n) + \frac{1}{4}y(n-1) = x(n) + \frac{1}{2}x(n-1)$. (1). Find the system function $H(z)$ and give the corresponding region of convergence. (2). Find the unit impulse response of the system.

7
